## COT 54005: Advanced Algorithms Fall 2006

## Assignment 2

1. (10 points) Show all steps involved in finding the 4 th smallest number from the following list of numbers, using the randomized selection algorithm discussed in class:
1514131216101711 . Use the following random sequence, with elements in $(0,1)$ :
$\begin{array}{lllll}0.9 & 0.1 & 0.5 & 0.8 & 0.7\end{array}$
2. (10 points) Construct a finite automaton for the pattern: 00101 and illustrate its operation on the text string 1100010100100101001.
3. (10 points) Construct a layered range tree for the following set of points: $\{(2,8),(8,4),(7,7)$, $(3,2),(4,10),(5,5),(6,6)\}$, using the procedure discussed in class. Show the steps involved in searching for all points in the following range: [2.8,6]x[4,9].
4. (10 points) Let $A$ be a three-dimensional $n \times n \times n$ array stored in row major order, as in $\mathrm{C} / \mathrm{C}++$. Give two algorithms that print all the elements of $A$, one of them having cache complexity $O\left(n^{3}\right)$ and another $O\left(n^{3} / L\right)$, under the ideal cache model.
5. (10 points) Problem 32.4-5 from CLR. Give a linear time algorithm to determine if a text $T$ is a cyclic rotation of another string $T^{\prime}$. For example, arc and car are cyclic rotations of each other.
