# FSU COP 4530 / CGS 5425 (Spring 2008) Data Structures, Algorithms, and Generic Programming 

## Due Feb 13

Assignment 3: Max points: 50

Please show steps or give justifications for all your answers, unless we specify otherwise. Each question is worth 5 points.

1. Assume that the time complexity of an algorithm on input of size $n$ is $2 n^{3}$. If the algorithm takes seconds to execute on some computer, on an input of size $n$, then how many seconds will it take on an input of size $3 n$ ?
2. Let the time complexity of an algorithm be: $2 n^{4} \log n+3 n^{4}-8 n^{2}+1000 \log n-1$. Give the asymptotic time in big-Oh notation. (You need not show steps.)
3. Show that $\mathrm{n}^{3}+2 \mathrm{n}^{2}$ is $\mathrm{O}\left(\mathrm{n}^{3}\right)$ directly from the definition of big-O, by finding appropriate constants C and N .
4. If $f(n)=O(k g(n))$ for some positive constant $k$, then prove, using the definition of Big-O, that $f(n)=$ $O(g(n))$.
5. If $f_{1}(n)=O\left(g_{1}(n)\right)$ and $f_{2}(n)=O\left(g_{2}(n)\right)$, then show that $f_{1}(n)-f_{2}(n)$ is not necessarily $O\left(g_{1}(n)-g_{2}(n)\right)$.
6. Draw the state of a self-organizing doubly linked list (count method) after the following operations. Show the links and counts too.
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insert(a); insert(b), insert(c), search(c), search(c), search(b)
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7. Which container, among those we have discussed (vector, sorted vector, singly linked list, or doubly linked list), will you use to store a set of student records? Assume that the following operations are performed: insert a record (making sure that multiple records are not inserted for the same student), delete the record of a student, or search for the record of a student. Justify your answer by comparing the time and space complexities of each container. Specify any assumptions that you make, such as assumptions regarding the relative likelihood of different operations.
8. Give the average number of comparisons in sequential search, with the following probability distribution. Prob (searching for element at location 0 ) $=1 / 3$, Prob(searching for element $i$ ) $=1 /(3[n-1])$, $1 \leq$ $i<n . \operatorname{Prob}($ element not found) $=1 / 3$.
9. In vector push_back, instead of doubling the capacity each time that the current capacity is exceeded, assume that we make it three times the current capacity. What is the amortized time complexity for n push_backs, assuming that the initial capacity was 1 ?
10. Using integration, give good upper and lower bounds on $\Sigma^{n}{ }_{i=1} i \sqrt{ } i^{-}$.
