

# Blockcipher

Viet Tung Hoang

Some slides are based on material from Prof. Mihir Bellare (UCSD) and Prof. Stefano Tessaro (UW)

# Agenda

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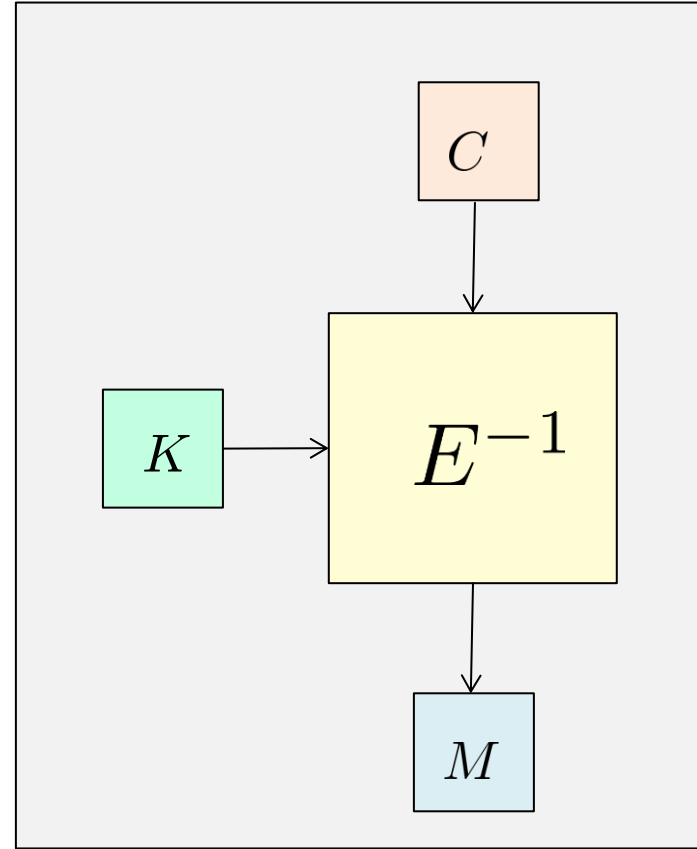
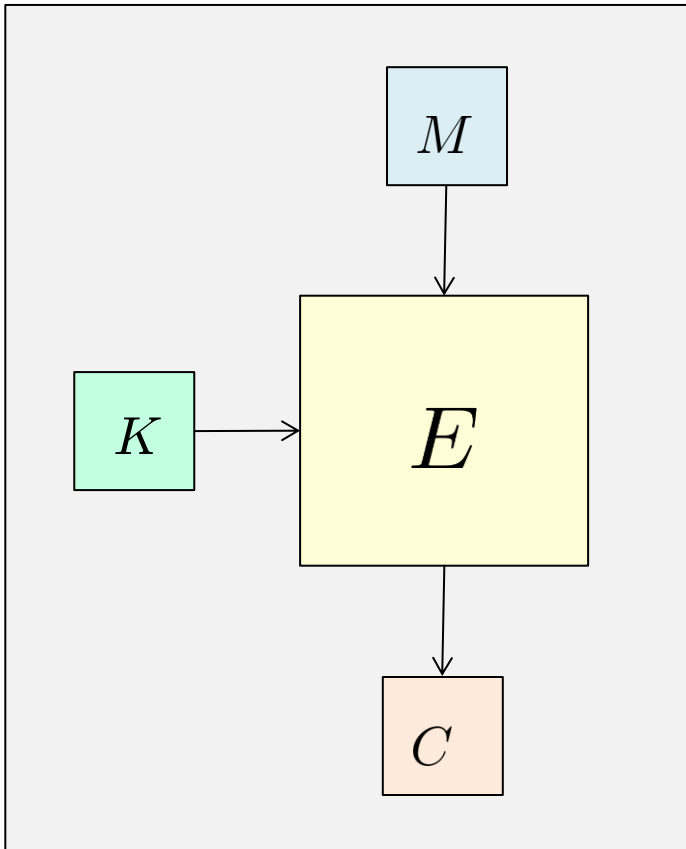
**1. Blockciphers**

2. Birthday Attack

# Blockcipher

efficiently invertible given the key

$$E : \underbrace{\{0, 1\}^k}_{\text{Key space}} \times \underbrace{\{0, 1\}^n}_{\text{Domain}} \rightarrow \{0, 1\}^n$$



# Blockcipher Usage



$$C_1 \leftarrow E_K(M_1)$$

...

$$C_q \leftarrow E_K(M_q)$$



$K$

$K$



Random key  $K$  is known to both parties, but not given to adversary  $A$

# Real-world Blockciphers

NIST Special Publication 800-67  
Version 1.1

**NIST**

**National Institute of  
Standards and Technology**  
Technology Administration  
U.S. Department of Commerce

Recommendation for the Triple  
Data Encryption Algorithm  
(TDEA) Block Cipher  
Revised 19 May 2008

William C. Barker

3DES, deprecated since 2017  
but still in legacy software  
 $k = 168, n = 64$

## FIPS 197

Federal Information Processing Standards Publication

## Advanced Encryption Standard (AES)

Category: Computer Security

Subcategory:

Information Technology Laboratory  
National Institute of Standards and Technology  
Gaithersburg, MD 20899-8900

AES, national standard  
 $k \in \{128, 192, 256\}, n = 128$

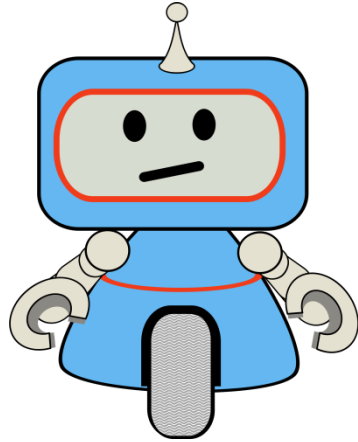
# Defining Security for Blockcipher

Possible Properties	Necessary	Sufficient
Hard to recover the key	Yes	No
Hard to find $M$ given $C \leftarrow E_K(M)$	Yes	No
...		

**Want:** a single “master” property that is sufficient to ensure security of common usage of blockcipher.

# An Analogy: Turing Test

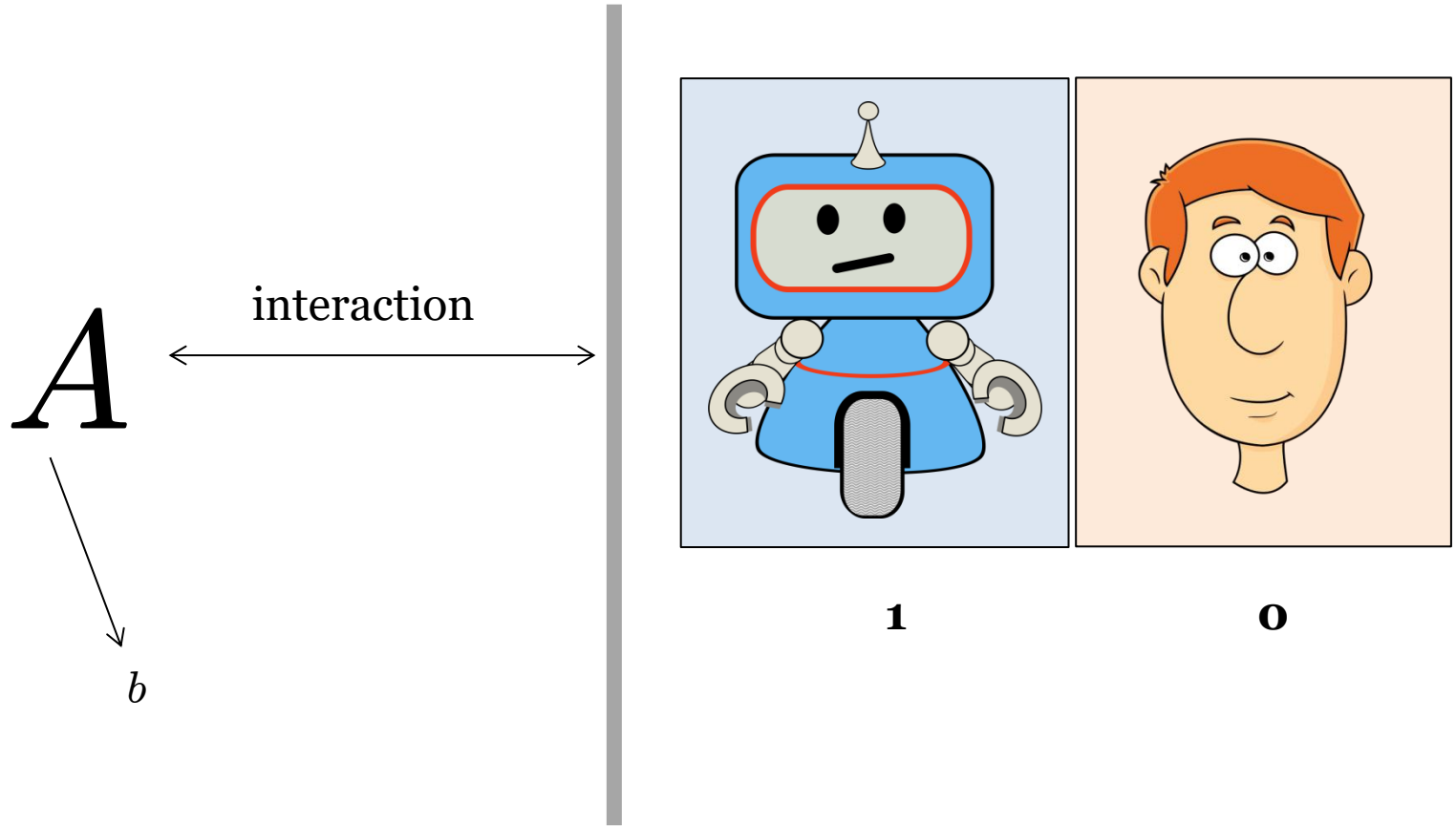
What does it mean for a machine to be “intelligent”?



Possible Answers
It can be happy
It recognizes pictures
...

But no such list is satisfactory

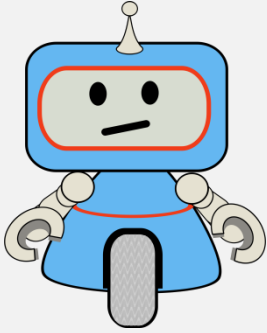

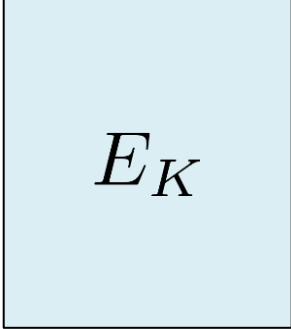
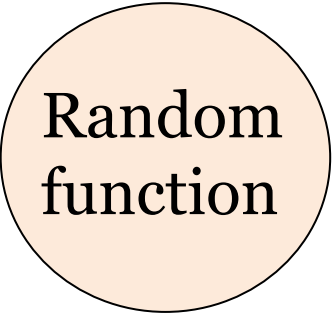
# An Analogy: Turing Test



Man (0) or Machine (1)?

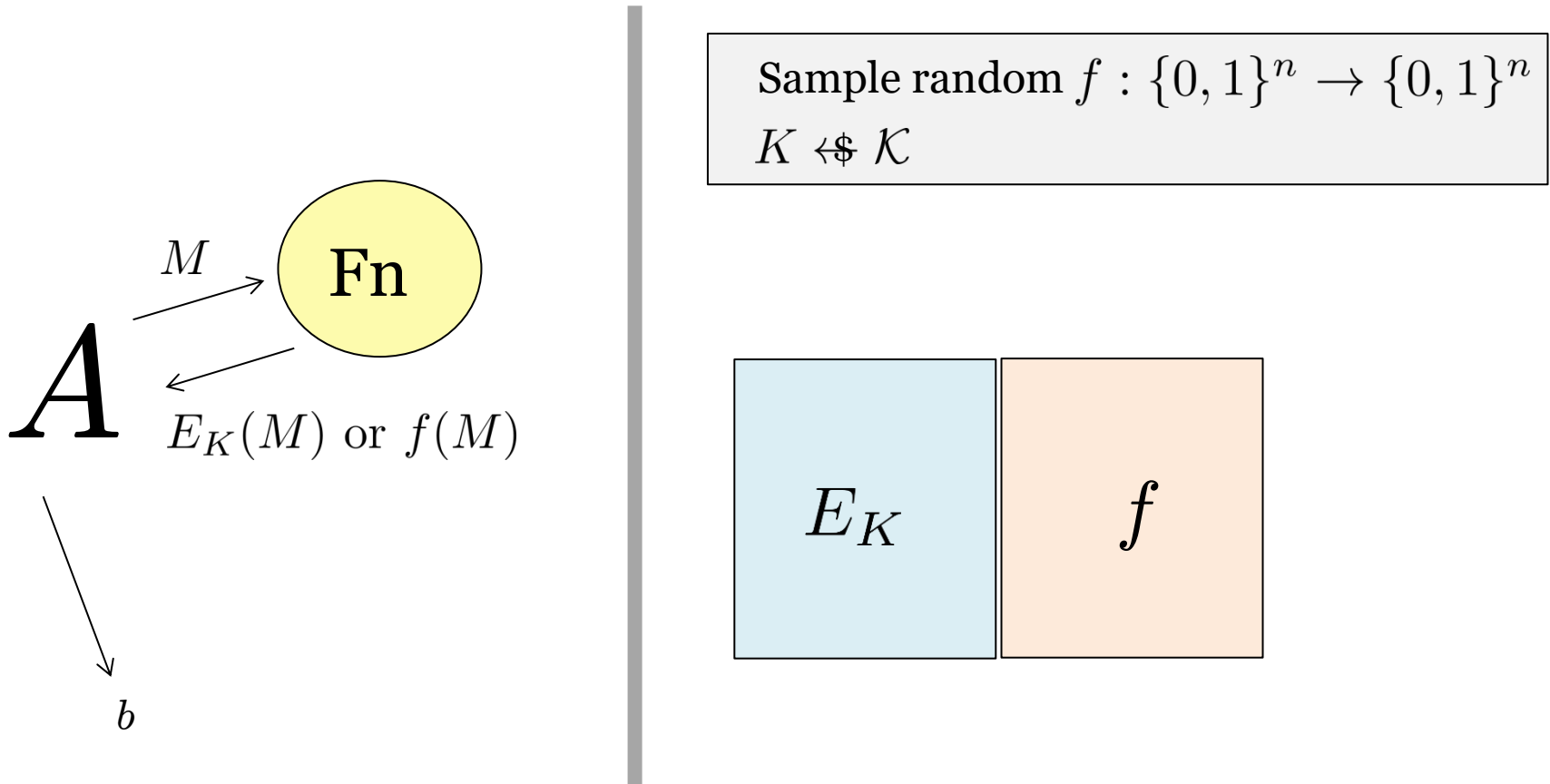


# Real versus Ideal

<b>Notion</b>	<b>Real object</b>	<b>Ideal object</b>
Intelligence		
PRF		

# Informal View of PRF Security

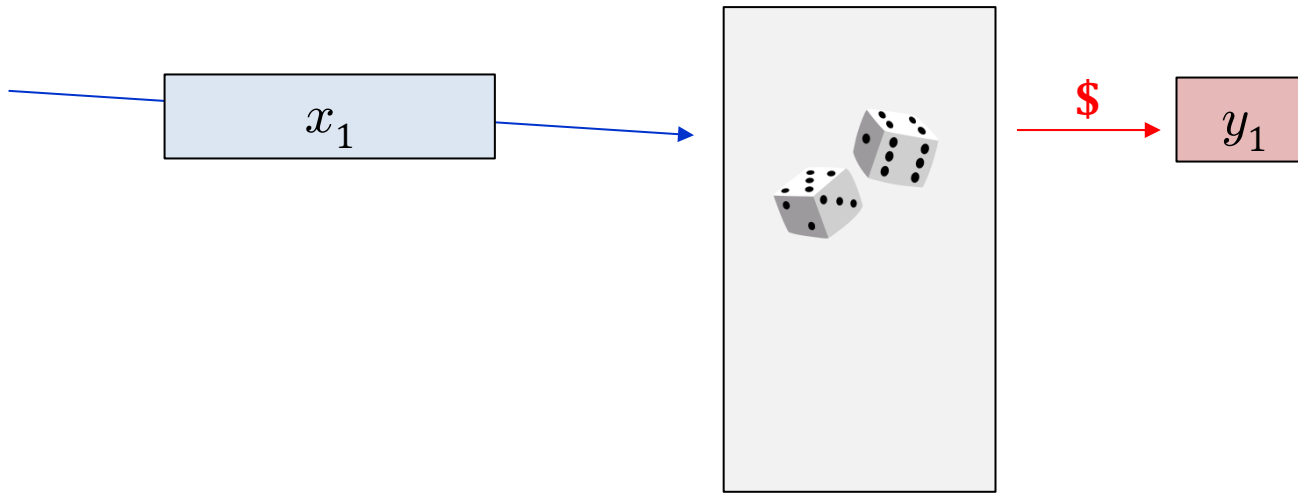
$$E : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$$



Adversary doesn't know  $K$  or  $f$

# Defining Random Function: Lazy Sampling

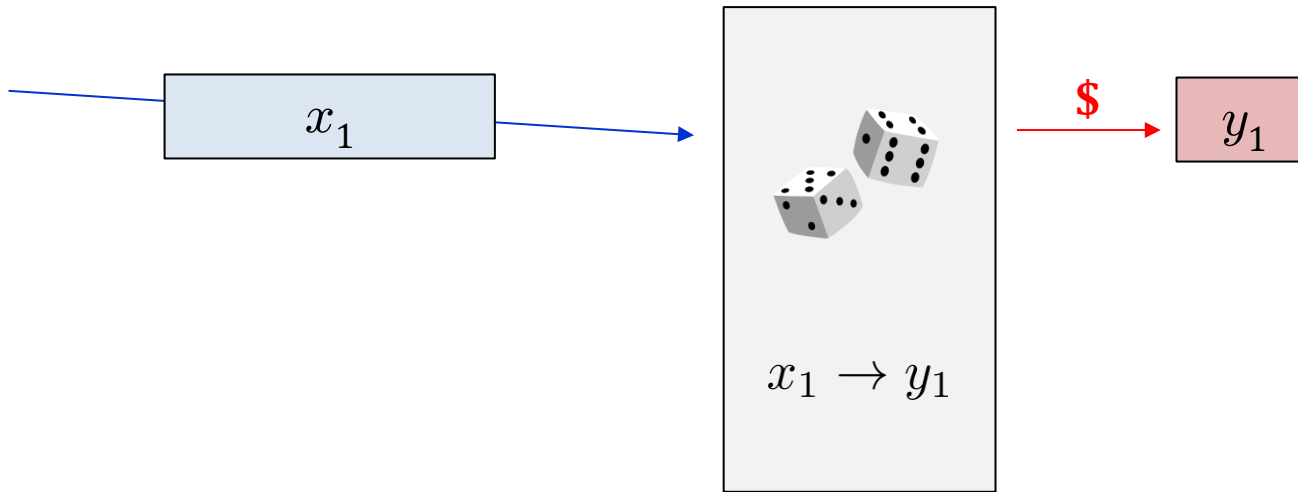
**Want:** a **random** function  $f : \{0, 1\}^n \rightarrow \{0, 1\}^m$



Pick a fresh random answer for a new query, and remember the answer

# Defining Random Function: Lazy Sampling

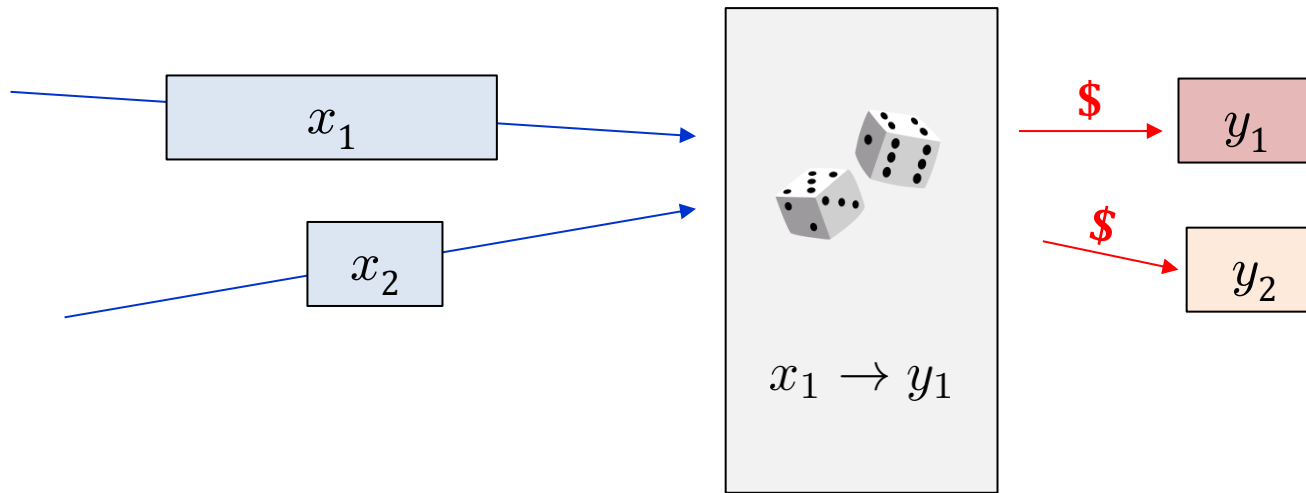
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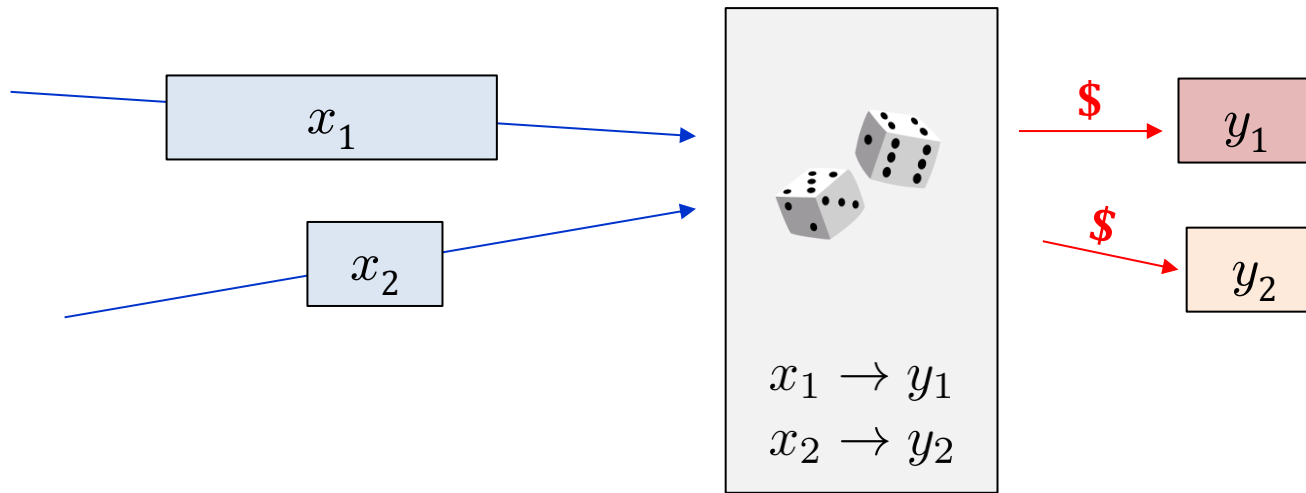
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# Defining Random Function: Lazy Sampling

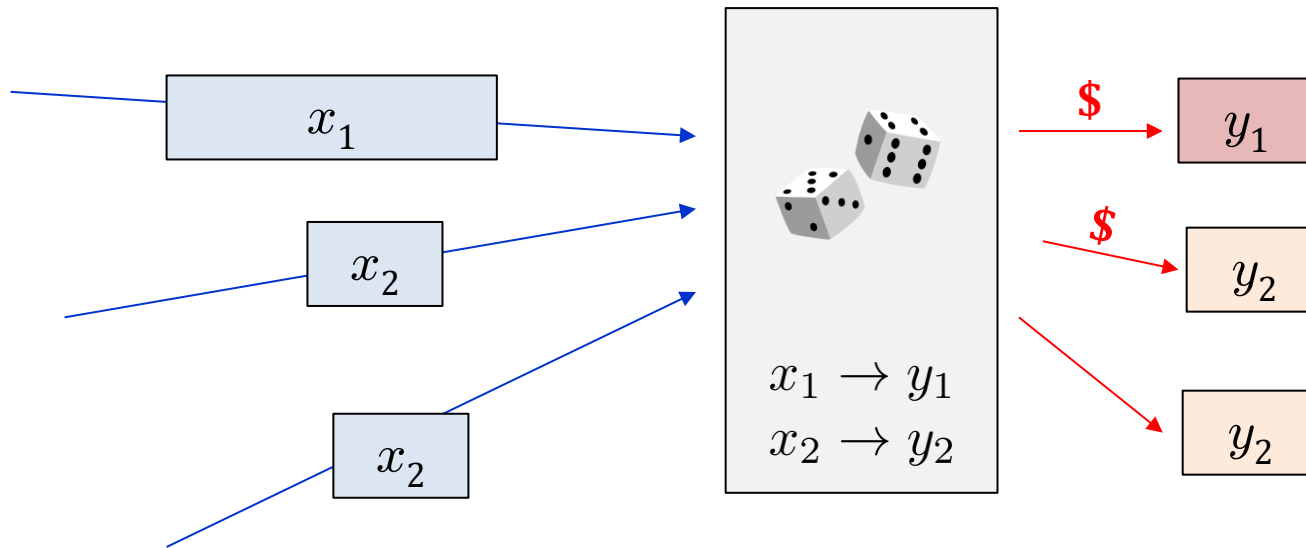
**Want:** a **random** function  $f : \{0, 1\}^n \rightarrow \{0, 1\}^m$



Pick a fresh random answer for a new query, and remember the answer

# Reuse Prior Answer for Old Query

Want: a **random** function  $f : \{0, 1\}^n \rightarrow \{0, 1\}^m$



# Putting Things in Code

**Game**  $\text{Real}_E$

**procedure** Initialize()

$K \leftarrow \$ \mathcal{K}$

**procedure** Fn( $M$ )

return  $E_K(M)$

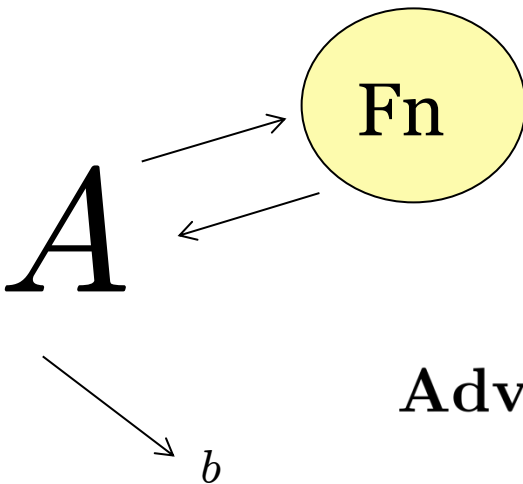
**Game**  $\text{Rand}_E$

string array  $T = \{\}$  // Global variable

**procedure** Fn( $M$ )

If  $T[M] = \perp$  then  $T[M] \leftarrow \$ \{0, 1\}^n$

return  $T[M]$

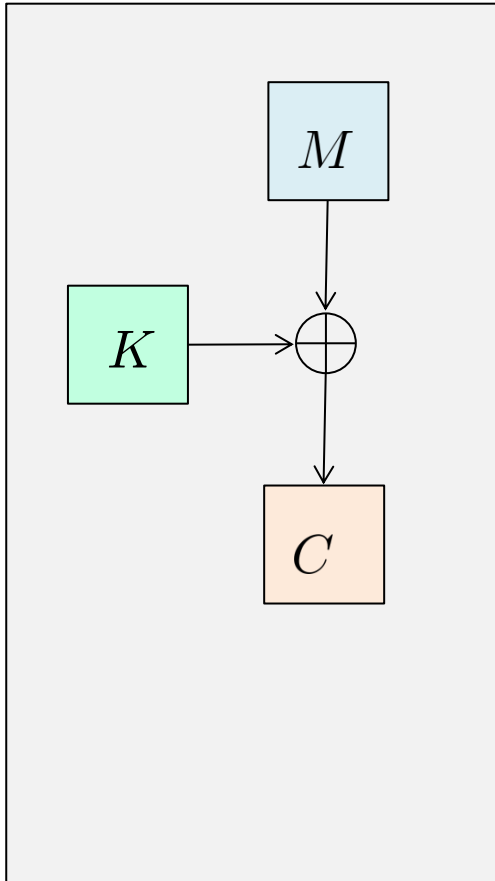


$$\text{Adv}_E^{\text{prf}}(A) = \Pr[\text{Real}_E^A \Rightarrow 1] - \Pr[\text{Rand}_E^A \Rightarrow 1]$$

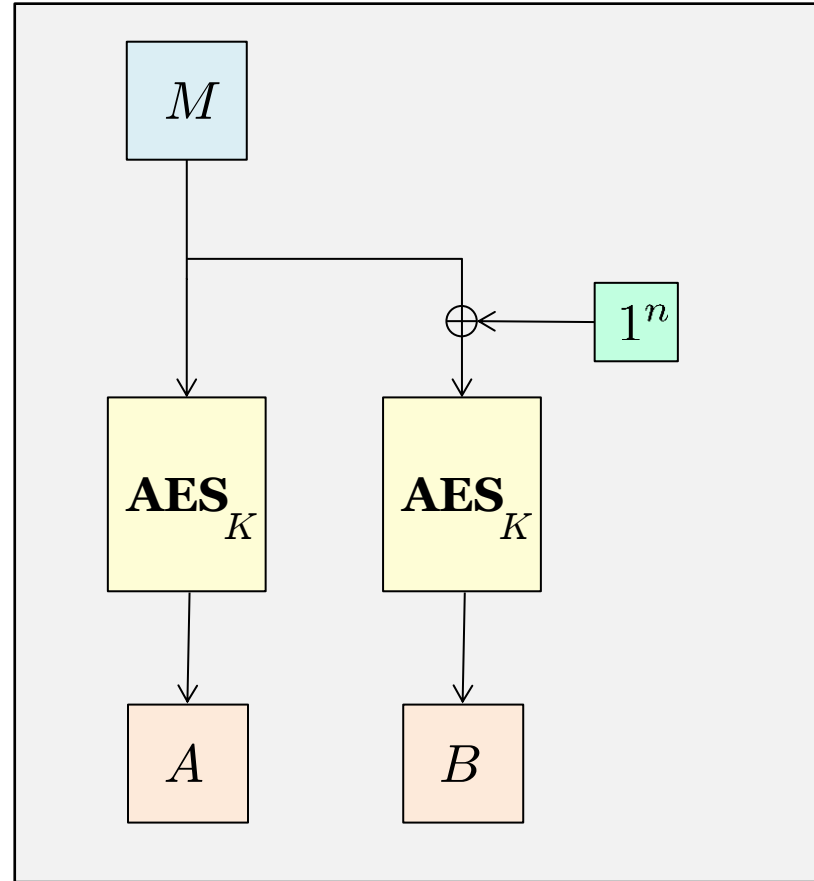


# Exercise: PRF Attacks

$$E_K(M) = M \oplus K$$



$$E_K(M) = \text{AES}_K(M) \parallel \text{AES}_K(\overline{M})$$



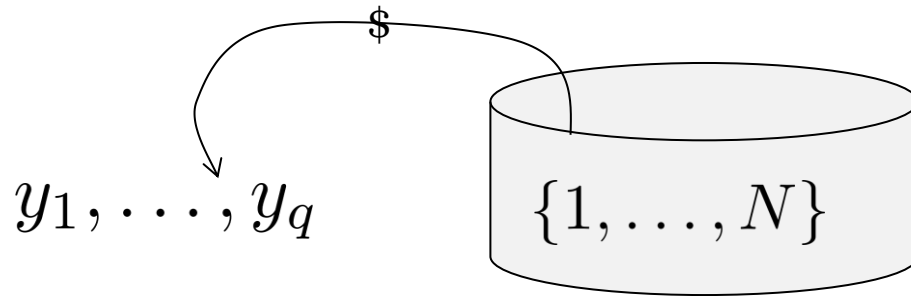
# Agenda

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1. Blockciphers

**2. Birthday Attack**

# Birthday Problem

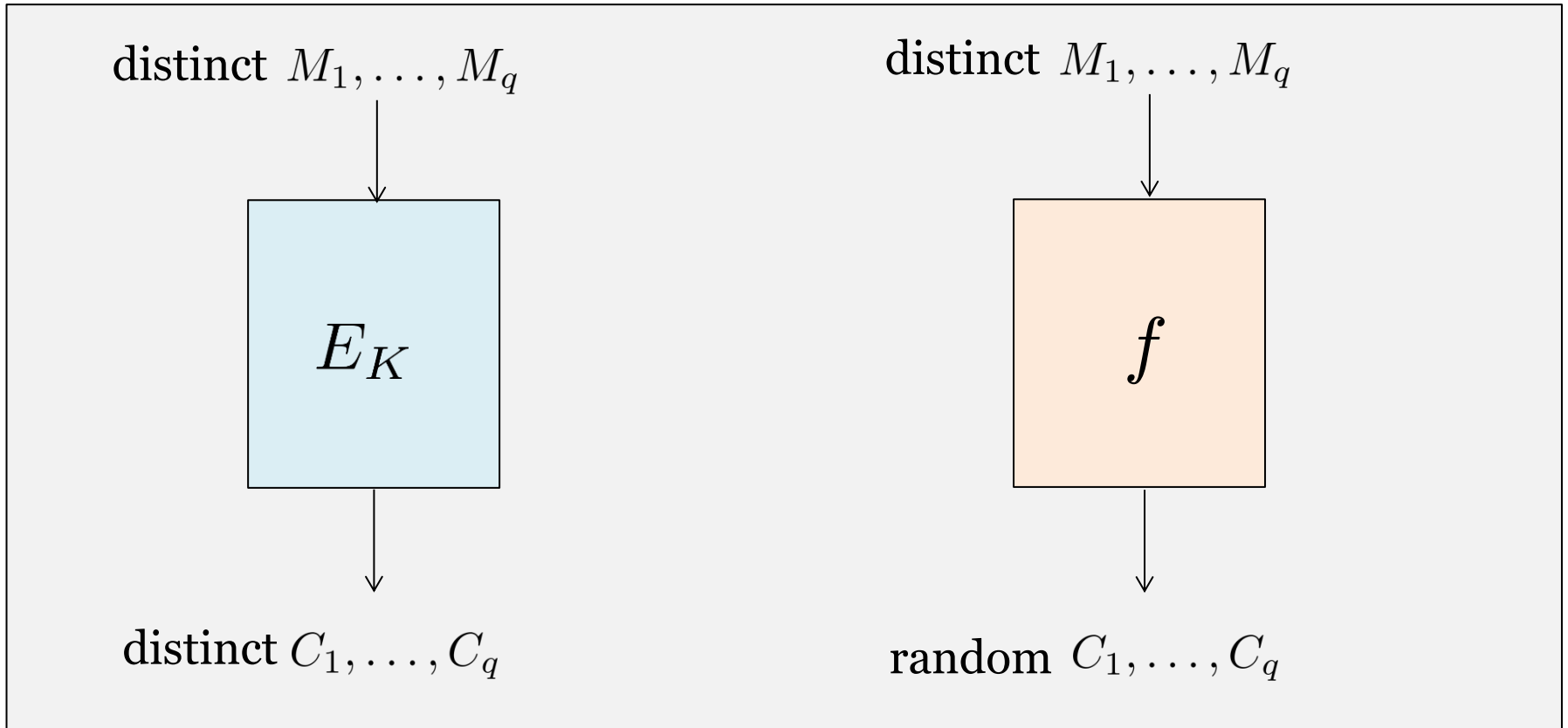


$$C(N, q) = \Pr[y_1, \dots, y_q \text{ not distinct}]$$

**Fact:** For  $q \leq \sqrt{2N}$ ,

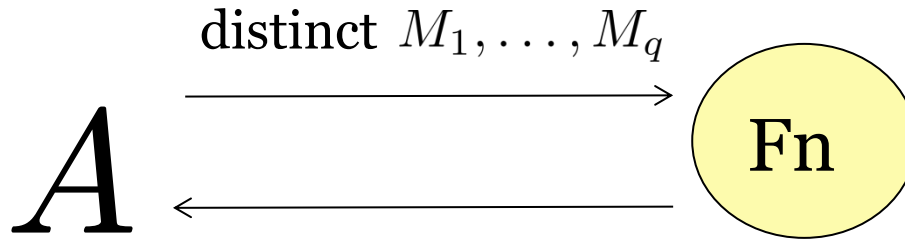
$$\frac{q(q-1)}{4N} \leq C(N, q) \leq \frac{q(q-1)}{2N}$$

# Birthday Attack on PRF Security



# Birthday Attack on PRF Security

$$E : \{0, 1\}^k \times \{0, 1\}^n \rightarrow \{0, 1\}^n$$



Output 1 if  $C_1, \dots, C_q$  are distinct

$$\text{Adv}_E^{\text{prf}}(A) = C(2^n, q) \approx \frac{q^2}{2^n}$$

Need  $2^{n/2}$  queries to break PRF security

Blockcipher	$n$	$2^{n/2}$	Status
3DES	64	$2^{32}$	Insecure
AES	128	$2^{64}$	Secure

# Does It Matter In Practice?

## Sweet32: Birthday Attacks on 64-bit Blockciphers in TLS and OpenVPN

[Bhargavan, Leurent 16]



HTTPS encryption via 3DES



Recover cookie after capturing 785GB